Mathematics

Grade(s) 11th - 12th, Duration 1 Year, 1 Credit Elective Course

#### **Course Overview**

This course is designed for students who expect to study engineering, economics, mathematics or physical sciences in college. The students will be taught in preparation for the AP Calculus AB exam and will have the opportunity to take that test at their expense.

# Scope And Sequence

Timeframe	Unit	Instructional Topics
4 Week(s)	Functions and Limits	Review of Functions     Continuity     Limits     Existance Theorems
9 Week(s)	The Derivative and its Applications	1. Average Rate of Change 2. Definition of the Derivative 3. Behavior of a function and its derivative 4. Relative Extrema 5. Absolute Extrema 6. Differentiation Rules 7. Implicit Differentiation 8. The second derivative 9. Mean Value Theorem and Tangent Line Approximations
9 Week(s)	The Integral - definitions and applications	Basic Integration Rules     Velocity Graphs     Riemann Sums     The Area Function
5 Week(s)	Applications of Integration	Volumes of solids with cross sections     Solids of Revolution     Differential Equations     Slope Fields
4 Week(s)	Review for AP Exam	

#### **Materials and Resources**

Rogawski: Calculus, Early Transcendentals

PLHSAPCalculus - blackboard

#### **Prerequisites**

Successful completion of Trigonometry and Analysis and teacher approval.

#### **Course Details**

Unit: Functions and Limits

Duration: 4 Week(s)

#### **Unit Overview**

The unit will cover the algebraic, graphical and numerical representations of limits.

#### **Academic Vocabulary**

Domain

Range

Continuity

Limits

Intermediate Value Theorem

Extreme Value Theorem

Infinite Limits

Asymptotes

Piecewise functions

**Topic:** Review of Functions Duration: 3 Day(s)

#### **Topic Overview**

Function Notation

Domain and Range

Odd and Even Functions

Transformations of functions: analytically, verbally, numerically and graphically

Composition of functions

Piecewise functions

Topic: Continuity Duration: 2 Day(s)

Mathematics

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**Topic Overview** 

Verifying Continuity
Graphical properties of continuity

Topic: Limits Duration: 6 Day(s)

**Topic Overview** 

Limits of Algebraic and Trigonometric Functions: numerically and graphically Infinite Limits: Asymptotic behavior Limits at Infinity: Horizontal Asymptotes

One Sided Limits

Topic: Existance Theorems Duration: 1 Day(s)

**Topic Overview** 

Intermediate Value Theorem Extreme Value Theorem

Unit: The Derivative and its Applications

Duration: 9 Week(s)

**Unit Overview** 

This unit will define the derivative. Investigate functions and their derivatives algebraically and graphically.

**Academic Vocabulary** 

Difference Quotients

Average Velocity

Instantaneous Rate of Change

Critical Numbers

Relative Extrema

Absolute Extrema

Related Rates

Acceleration

Parametric Equations

Chain Rule

Tangent Lines

Secant Lines

Mean Value Theorem

**Topic:** Average Rate of Change **Duration:** 2 Day(s)

**Topic Overview** 

Difference Quotients from Data, Graphical Displays

Average Velocity as change in position/time

**Topic:** Definition of the Derivative **Duration**: 4 Day(s)

**Topic Overview** 

Defintion of Derivative (limiting value of average rate of change)

Secant lines vs tangent lines

Instantaneous Rate of Change

**Topic:** Behavior of a function and its derivative **Duration**: 2 Day(s)

**Topic Overview** 

Investigate function both alegebraically and graphically that confirm the behavior of a function and its derivaitve.

**Topic:** Relative Extrema **Duration**: 2 Day(s)

Mathematics

Grade(s) 11th - 12th, Duration 1 Year, 1 Credit
Flective Course

**Topic Overview** 

Locating critical numbers Using the derivative to determine extrema Sketching the dertivative based upon the function

Topic: Absolute Extrema Duration: 4 Day(s)

**Topic Overview** 

Closed intervals
Applied Max/Min Problems

**Topic:** Differentiation Rules **Duration:** 5 Day(s)

**Topic Overview** 

Power, Constant Multiple, Sum, Product and Quotient Rules Transcendental Rules Chain Rule Higher Order derivatives, Acceleration

**Topic:** Implicit Differentiation **Duration:** 4 Day(s)

**Topic Overview** 

Parametric Equations Chain Rule in Parametic Form Related Rates

Topic: The second derivative Duration: 3 Day(s)

**Topic Overview** 

Concavity Second Derivative Test Points of Inflection

**Topic:** Mean Value Theorem and Tangent Line Approximations **Duration:** 3 Day(s)

**Topic Overview** 

Using MVT and Tangent Line approximations

Unit: The Integral - definitions and applications

Duration: 9 Week(s)

**Unit Overview** 

Understanding the integral and its relationship to the derivative.

Academic Vocabulary

Average Value of a Function

Riemann Sums

Integration

Anti Derivatives

First Fundamental Theorem of Calculus

Second Fundamental Theorem of Calculus

u-substitution

Topic: Basic Integration Rules Duration: 4 Day(s)

**Topic Overview** 

Integration Rules U-substitution

**Topic:** Velocity Graphs **Duration:** 6 Day(s)

Mathematics

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Flective Course

**Topic Overview** 

Distance traveled vs displacement Area Under the Curve 2nd Fundamental Theorem of Calculus

Topic: Riemann Sums Duration: 6 Day(s)

**Topic Overview** 

Left Hand Right Hand Trapezoidal

Riemann Sums to approximate

Equal and Unequal subdivisions

**Topic:** The Area Function **Duration:** 6 Day(s)

**Topic Overview** 

First Fundamental Theorem of Calculus Area functions vs riemann sum Area of discrete functions

Unit: Applications of Integration Duration: 5 Week(s)

**Unit Overview** 

Advanced application of integraion

**Academic Vocabulary** 

Solids of Revolution - disks, washers

Logistics Curve Differential Equations

Slope Fields

**Topic:** Volumes of solids with cross sections **Duration:** 3 Day(s)

**Topic Overview** 

Find the volume of solids with known cross-sections

Topic: Solids of Revolution Duration: 6 Day(s)

**Topic Overview** 

Disc Method Washer Method

**Topic:** Differential Equations **Duration:** 4 Day(s)

**Topic Overview** 

Seperation of Variables Initial Conditions

**Topic:** Slope Fields **Duration:** 2 Day(s)

**Topic Overview** 

Defining Slope Fields

Determining a function based upon the slope field

Unit: Review for AP Exam

Duration: 4 Week(s)

# **Calculus - Advanced Placement (AP)**Mathematics

Grade(s) 11th - 12th, Duration 1 Year, 1 Credit Elective Course

**Unit Overview** 

Review all concepts and take practice exams using released AP material

**Duration:** Topic: